Homework 4

1. (a) Consider the following LR grammar:

\[
E \rightarrow E + T \mid E - T \mid T \\
T \rightarrow T * F \mid T/F \mid F \\
F \rightarrow (E) \mid \text{id}
\]

Give a rightmost derivation and parse tree for the following expression:
(id*id) + (id - id) / id

(b) Now consider an equivalent LL grammar:

\[
E \rightarrow TE' \\
E' \rightarrow +TE' \mid -TE' \mid \epsilon \\
T \rightarrow FT' \\
T' \rightarrow *FT' \mid /FT' \mid \epsilon \\
F \rightarrow (E) \mid \text{id}
\]

Give a leftmost derivation and parse tree for the same expression:
(id*id) + (id - id) / id

2. Consider the following LL grammar:

\[
S \rightarrow aB \mid bA \mid \epsilon \\
A \rightarrow bAA \mid aS \\
B \rightarrow aBB \mid bS
\]

(a) Compute the FIRST and FOLLOW sets for each nonterminal.

(b) Using the FIRST and FOLLOW sets, generate the predictive parsing table.

(c) Show the parsing action (including the matches, stack, input and action columns) for the string: baaabb. Note that your parsing will not actually accept this one; you should simply show the parsing action up to the point where it gets stuck.

(d) Extra credit: Show a string (with at least 5 characters in it) that IS accepted by some parsing action for the table you generated in part (b).

3. Show that the following grammar is not LL:

\[
A \rightarrow Ac \mid Aad \mid bd \mid \epsilon
\]