

# Machine-Level Programming II: Control and Arithmetic

CSCI 2400: Computer Architecture

**Instructor:**

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*Slides adapted from Bryant & O'Hallaron's slides*

# Today

- Complete addressing mode, address computation (`leal`)
- Arithmetic operations
- x86 Calling Convention (functions)
- Control: Condition codes
- Conditional branches
- While loops

# Complete Memory Addressing Modes

- Most General Form
- $D(Rb, Ri, S) \quad \text{Mem[Reg[Rb]+S*Reg[Ri]]+ D}$ 
  - D: Constant “displacement” 1, 2, or 4 bytes
  - Rb: Base register: Any of 8 integer registers
  - Ri: Index register: Any, except for %esp
    - Unlikely you’d use %ebp, either
  - S: Scale: 1, 2, 4, or 8 (*why these numbers?*)
- Special Cases
- $(Rb, Ri) \quad \text{Mem[Reg[Rb]+Reg[Ri]]}$
- $D(Rb, Ri) \quad \text{Mem[Reg[Rb]+Reg[Ri]]+D}$
- $(Rb, Ri, S) \quad \text{Mem[Reg[Rb]+S*Reg[Ri]]}$

# Quick Check

$$D(Rb, Ri, S) = \text{Mem}[\text{Reg}[Rb] + S * \text{Reg}[Ri] + D]$$

%edx	0xf000
%ecx	0x0100

Expression	Address Computation	Address
0x8(%edx)		
(%edx, %ecx)		
(%edx, %ecx, 4)		
0x80(, %edx, 2)		

# Address Computation Instruction

## ■ **leal Src,Dest**

- *Src* is address mode expression
- Set *Dest* to address denoted by expression

## ■ **Uses**

- Computing addresses without a memory reference
  - E.g., translation of `p = &x[i];`
- Computing arithmetic expressions of the form  $x + k*y$ 
  - $k = 1, 2, 4, \text{ or } 8$

## ■ **Example**

```
int mul12(int x)
{
    return x*12;
}
```

Converted to ASM by compiler:

```
leal (%eax,%eax,2), %eax ; t <- x+x*2
sal1 $2, %eax             ; return t<<2
```

# Today

- Complete addressing mode, address computation (leal)
- **Arithmetic operations**
- x86 Calling Convention (functions)
- Control: Condition codes
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# Some Arithmetic Operations

## ■ Two Operand Instructions:

<i>Format</i>	<i>Computation</i>	
addl <i>Src,Dest</i>	Dest = Dest + Src	
subl <i>Src,Dest</i>	Dest = Dest – Src	
imull <i>Src,Dest</i>	Dest = Dest * Src	
sall <i>Src,Dest</i>	Dest = Dest << Src	<i>Also called shll</i>
sarl <i>Src,Dest</i>	Dest = Dest >> Src	<i>Arithmetic</i>
shrl <i>Src,Dest</i>	Dest = Dest >> Src	<i>Logical</i>
xorl <i>Src,Dest</i>	Dest = Dest ^ Src	
andl <i>Src,Dest</i>	Dest = Dest & Src	
orl <i>Src,Dest</i>	Dest = Dest   Src	

## ■ Watch out for argument order!

## ■ No distinction between signed and unsigned int (why?)

# Some Arithmetic Operations

## ■ One Operand Instructions

incl      *Dest*       $Dest = Dest + 1$

decl      *Dest*       $Dest = Dest - 1$

negl      *Dest*       $Dest = -Dest$

notl      *Dest*       $Dest = \sim Dest$

## ■ See book for more instructions

# Arithmetic Expression Example

```
int arith(int x, int y, int z)
{
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
}
```

arith:

pushl %ebp  
movl %esp, %ebp

}

Set Up

movl 8(%ebp), %ecx  
movl 12(%ebp), %edx  
leal (%edx,%edx,2), %eax  
sall \$4, %eax  
leal 4(%ecx,%eax), %eax  
addl %ecx, %edx  
addl 16(%ebp), %edx  
imull %edx, %eax

Body

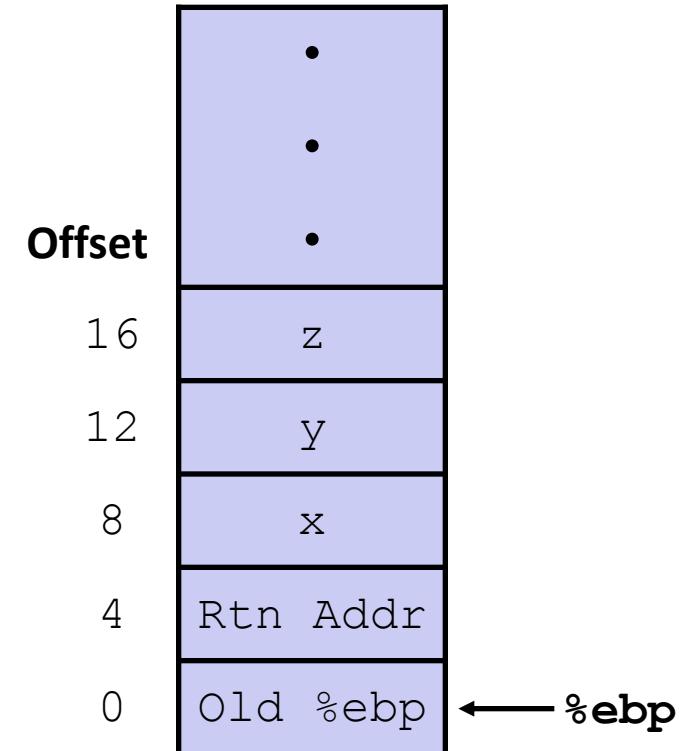
popl %ebp  
ret

}

Finish

# Understanding arith

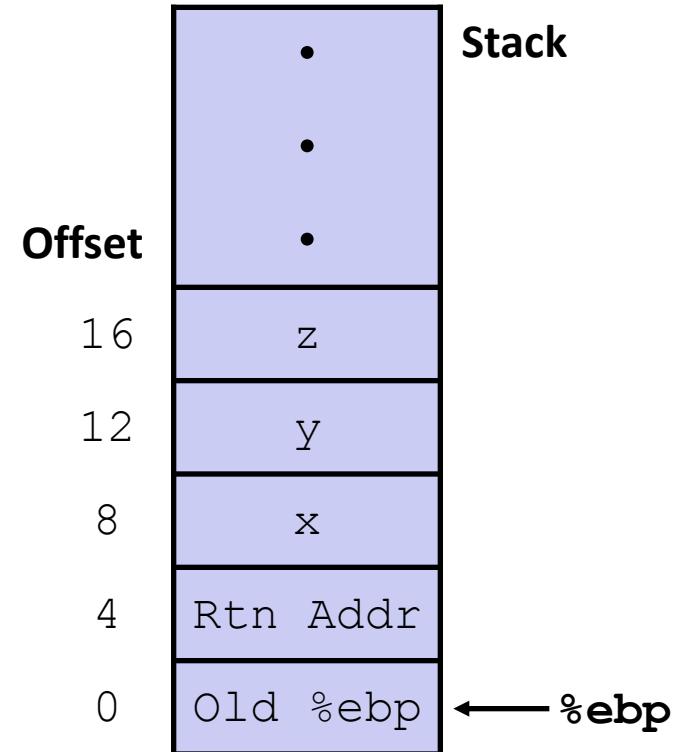
```
int arith(int x, int y, int z)
{
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
}
```



```
movl 8(%ebp), %ecx
movl 12(%ebp), %edx
leal (%edx,%edx,2), %eax
sall $4, %eax
leal 4(%ecx,%eax), %eax
addl %ecx, %edx
addl 16(%ebp), %edx
imull %edx, %eax
```

# Understanding arith

```
int arith(int x, int y, int z)
{
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
}
```



movl 8(%ebp), %ecx	# ecx = x
movl 12(%ebp), %edx	# edx = y
leal (%edx,%edx,2), %eax	# eax = y*3
sall \$4, %eax	# eax *= 16 (t4)
leal 4(%ecx,%eax), %eax	# eax = t4 +x+4 (t5)
addl %ecx, %edx	# edx = x+y (t1)
addl 16(%ebp), %edx	# edx += z (t2)
imull %edx, %eax	# eax = t2 * t5 (rval)

# Observations about arith

```
int arith(int x, int y, int z)
{
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
}
```

- Instructions in different order from C code
- Some expressions require multiple instructions
- Some instructions cover multiple expressions
- Get exact same code when compile:
- $(x+y+z) * (x+4+48*y)$

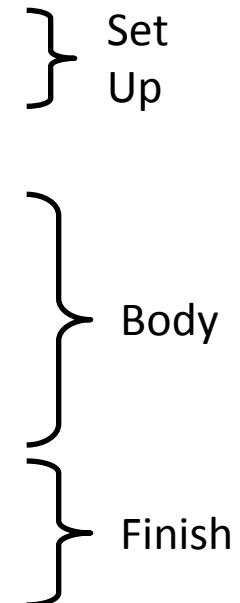
movl 8(%ebp), %ecx	# ecx = x
movl 12(%ebp), %edx	# edx = y
leal (%edx,%edx,2), %eax	# eax = y*3
sall \$4, %eax	# eax *= 16 (t4)
leal 4(%ecx,%eax), %eax	# eax = t4 +x+4 (t5)
addl %ecx, %edx	# edx = x+y (t1)
addl 16(%ebp), %edx	# edx += z (t2)
imull %edx, %eax	# eax = t2 * t5 (rval)

# Another Example

```
int logical(int x, int y)
{
    int t1 = x^y;
    int t2 = t1 >> 17;
    int mask = (1<<13) - 7;
    int rval = t2 & mask;
    return rval;
}
```

logical:

```
pushl %ebp
movl %esp,%ebp
movl 12(%ebp),%eax
xorl 8(%ebp),%eax
sarl $17,%eax
andl $8185,%eax
popl %ebp
ret
```



<code>movl 12(%ebp),%eax</code>	# eax = y
<code>xorl 8(%ebp),%eax</code>	# eax = x^y (t1)
<code>sarl \$17,%eax</code>	# eax = t1>>17 (t2)
<code>andl \$8185,%eax</code>	# eax = t2 & mask (rval)

# Another Example

```
int logical(int x, int y)
{
    int t1 = x^y;
    int t2 = t1 >> 17;
    int mask = (1<<13) - 7;
    int rval = t2 & mask;
    return rval;
}
```

logical:

```
pushl %ebp  
movl %esp,%ebp
```

} Set Up

```
movl 12(%ebp),%eax  
xorl 8(%ebp),%eax  
sarl $17,%eax  
andl $8185,%eax
```

} Body

```
popl %ebp  
ret
```

} Finish

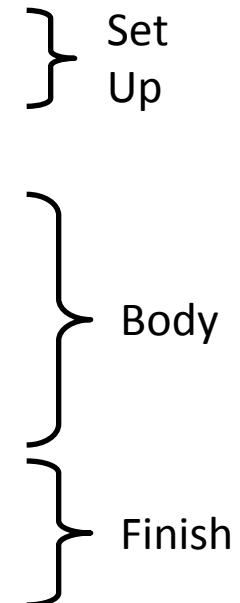
movl 12(%ebp),%eax	# eax = y
xorl 8(%ebp),%eax	# eax = x^y (t1)
sarl \$17,%eax	# eax = t1>>17 (t2)
andl \$8185,%eax	# eax = t2 & mask (rval)

# Another Example

```
int logical(int x, int y)
{
    int t1 = x^y;
    int t2 = t1 >> 17;
    int mask = (1<<13) - 7;
    int rval = t2 & mask;
    return rval;
}
```

logical:

```
pushl %ebp
movl %esp,%ebp
movl 12(%ebp),%eax
xorl 8(%ebp),%eax
sarl $17,%eax
andl $8185,%eax
popl %ebp
ret
```



movl 12(%ebp),%eax	# eax = y
xorl 8(%ebp),%eax	# eax = x^y (t1)
sarl \$17,%eax	# eax = t1>>17 (t2)
andl \$8185,%eax	# eax = t2 & mask (rval)

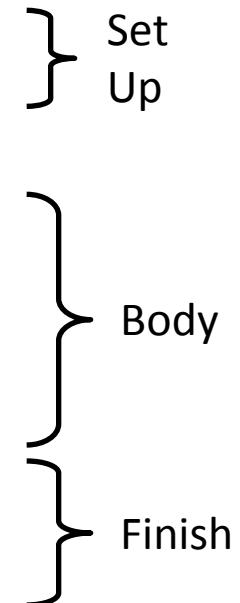
# Another Example

```
int logical(int x, int y)
{
    int t1 = x^y;
    int t2 = t1 >> 17;
    int mask = (1<<13) - 7;
    int rval = t2 & mask;
    return rval;
}
```

$$2^{13} = 8192, 2^{13} - 7 = 8185$$

logical:

```
pushl %ebp
movl %esp,%ebp
movl 12(%ebp),%eax
xorl 8(%ebp),%eax
sarl $17,%eax
andl $8185,%eax
popl %ebp
ret
```



<code>movl 12(%ebp),%eax</code>	# eax = y
<code>xorl 8(%ebp),%eax</code>	# eax = x^y (t1)
<code>sarl \$17,%eax</code>	# eax = t1>>17 (t2)
<code>andl \$8185,%eax</code>	# eax = t2 & mask (rval)

# Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- **x86 Calling Convention (functions)**
- Control: Condition codes
- Conditional branches
- While loops

# x86 Function Calling Conventions

- Functions are the basis for *code re-use*
- Calling a function interferes with the processor state
  - We have to worry about saving this state in assembly
  - Compiler handles the details in higher level languages
- A function is allowed (by convention) to modify:
  - EAX
  - ECX
  - EDI
- These are called *caller-saved*
- Return values from a function are stored in EAX

# x86 Argument Passing

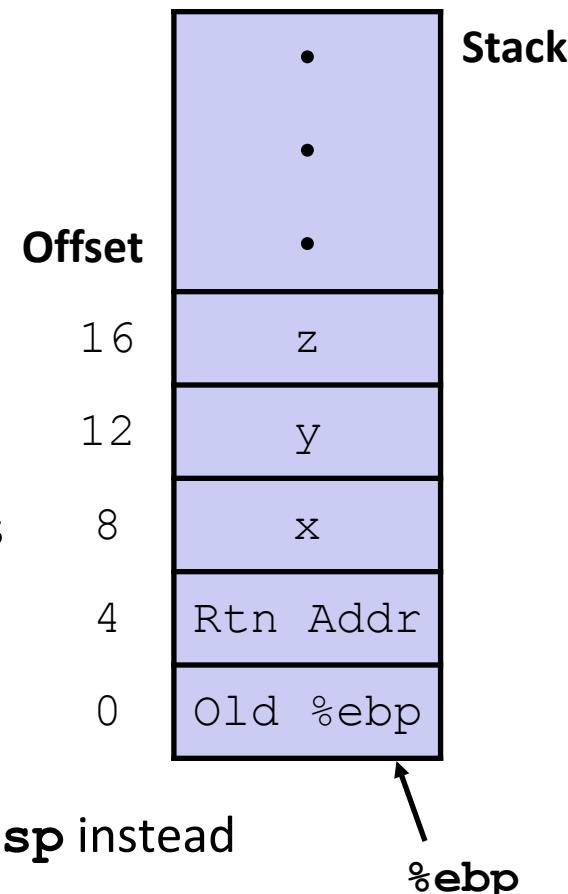
- Function arguments must be stored in registers or somewhere in memory

- X86 has relatively few registers
- The stack stores arguments in memory

- For example:

```
int arith(int x, int y, int z)
```

- Caller pushes values from right to left
- `call` instruction pushes function return address
- Callee pushes `ebp` in function preamble
- Callee accesses leftmost arguments as 8(%ebp)
  - Other arguments as 12, 16, and so on
- Compiler sometimes generates code that uses `esp` instead



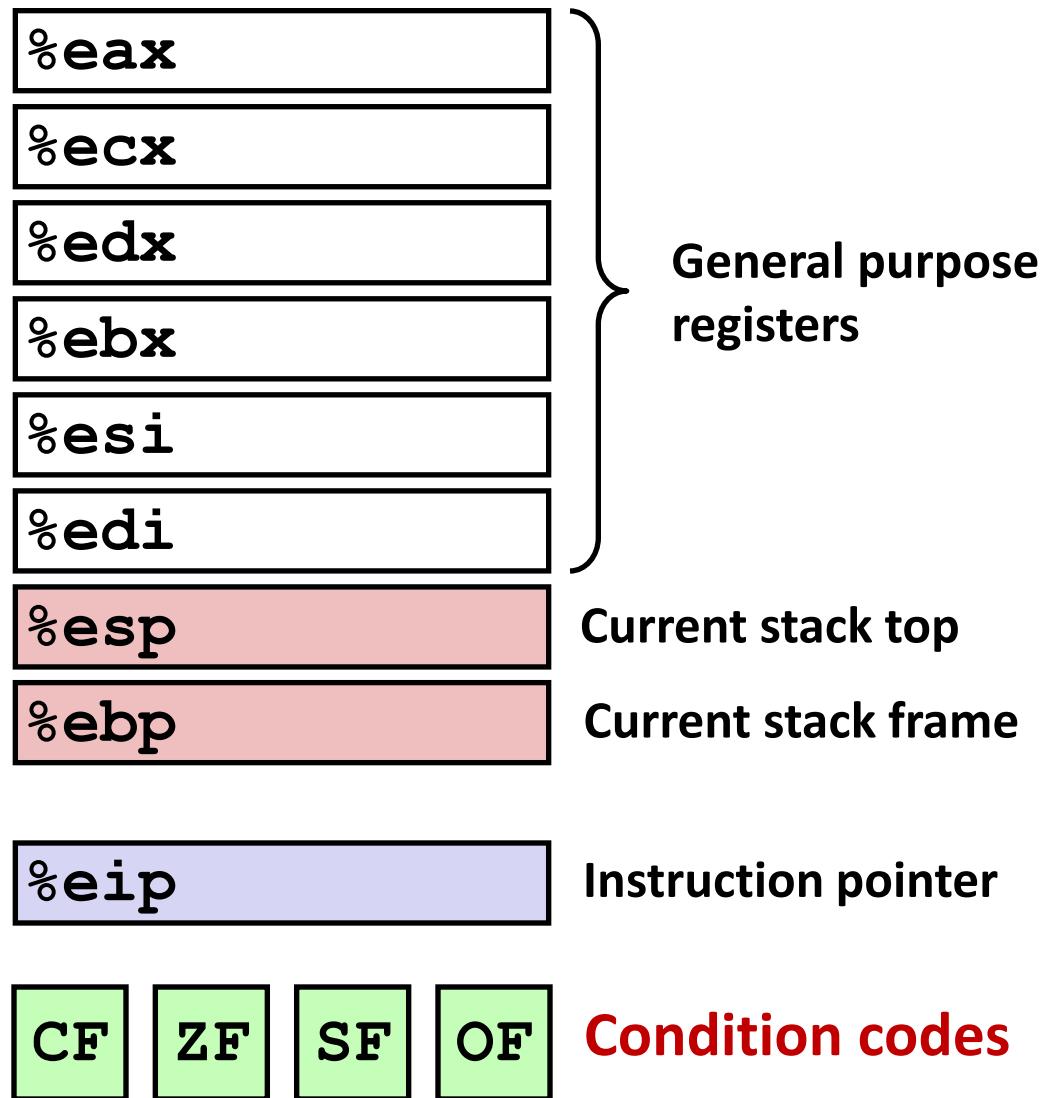
# Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86 Calling Convention (functions)
- **Control: Condition codes**
- Conditional branches
- Loops

# Processor State (IA32, Partial)

## ■ Information about currently executing program

- Temporary data ( `%eax`, ... )
- Location of runtime stack ( `%ebp`, `%esp` )
- Location of current code control point ( `%eip`, ... )
- Status of recent tests ( `CF`, `ZF`, `SF`, `OF` )



# Condition Codes (Implicit Setting)

## ■ Single bit registers

- CF Carry Flag (for unsigned) SF Sign Flag (for signed)
- ZF Zero Flag OF Overflow Flag (for signed)

## ■ Implicitly set (think of it as side effect) by arithmetic operations

Example: **addl/addq Src,Dest**  $\leftrightarrow t = a+b$

**CF set** if carry out from most significant bit (unsigned overflow)

**ZF set** if  $t == 0$

**SF set** if  $t < 0$  (as signed)

**OF set** if two's-complement (signed) overflow

$(a>0 \ \&\& \ b>0 \ \&\& \ t<0) \ || \ (a<0 \ \&\& \ b<0 \ \&\& \ t>=0)$

## ■ Not set by **le<sub>a</sub>** instruction

## ■ [Full documentation \(IA32\)](#), link on course website

# Condition Codes (Explicit Setting: Compare)

## ■ Explicit Setting by Compare Instruction

- **cmp1 / cmpq Src2, Src1**
- **cmpl b, a** like computing  $a - b$  without setting destination
  
- **CF set** if carry out from most significant bit (used for unsigned comparisons)
- **ZF set** if  $a == b$
- **SF set** if  $(a - b) < 0$  (as signed)
- **OF set** if two's-complement (signed) overflow  
$$(a>0 \ \&\& \ b<0 \ \&\& \ (a-b)<0) \ \|\ (a<0 \ \&\& \ b>0 \ \&\& \ (a-b)>0)$$

# Condition Codes (Explicit Setting: Test)

## ■ Explicit Setting by Test instruction

- `testl/testq Src2, Src1`

`testl b, a` like computing `a&b` without setting destination

- Sets condition codes based on value of `Src1 & Src2`

- Useful to have one of the operands be a mask

- **ZF set** when `a&b == 0`

- **SF set** when `a&b < 0`

# Reading Condition Codes

## ■ SetX Instructions

- Set single byte based on combinations of condition codes

SetX	Condition	Description
<b>sete</b>	<b>ZF</b>	<b>Equal / Zero</b>
<b>setne</b>	<b><math>\sim ZF</math></b>	<b>Not Equal / Not Zero</b>
<b>sets</b>	<b>SF</b>	<b>Negative</b>
<b>setns</b>	<b><math>\sim SF</math></b>	<b>Nonnegative</b>
<b>setg</b>	<b><math>\sim (SF \wedge OF) \ \&amp; \ \sim ZF</math></b>	<b>Greater (Signed)</b>
<b>setge</b>	<b><math>\sim (SF \wedge OF)</math></b>	<b>Greater or Equal (Signed)</b>
<b>setl</b>	<b><math>(SF \wedge OF)</math></b>	<b>Less (Signed)</b>
<b>setle</b>	<b><math>(SF \wedge OF) \mid ZF</math></b>	<b>Less or Equal (Signed)</b>
<b>seta</b>	<b><math>\sim CF \ \&amp; \ \sim ZF</math></b>	<b>Above (unsigned)</b>
<b>setb</b>	<b>CF</b>	<b>Below (unsigned)</b>

# Reading Condition Codes (Cont.)

## ■ SetX Instructions:

- Set single byte based on combination of condition codes

## ■ One of 8 addressable byte registers

- Does not alter remaining 3 bytes
- Typically use `movzbl` to finish job

```
int gt (int x, int y)
{
    return x > y;
}
```

## Body

```
movl 12(%ebp),%eax      # eax = y
cmpl %eax,8(%ebp)       # Compare x : y
setg %al                 # al = x > y
movzbl %al,%eax         # Zero rest of %eax
```

%eax	%ah	%al
------	-----	-----

%ecx	%ch	%cl
------	-----	-----

%edx	%dh	%dl
------	-----	-----

%ebx	%bh	%bl
------	-----	-----

%esi
------

%edi
------

%esp
------

%ebp
------

# Today

- Complete addressing mode, address computation (`leal`)
- Arithmetic operations
- x86 Calling Convention (functions)
- Control: Condition codes
- **Conditional branches & Moves**
- Loops

# Jumping

## ■ jX Instructions

- Jump to different part of code depending on condition codes

jX	Condition	Description
jmp	1	Unconditional
je	ZF	Equal / Zero
jne	~ZF	Not Equal / Not Zero
js	SF	Negative
jns	~SF	Nonnegative
jg	~(SF^OF) & ~ZF	Greater (Signed)
jge	~(SF^OF)	Greater or Equal (Signed)
jl	(SF^OF)	Less (Signed)
jle	(SF^OF)   ZF	Less or Equal (Signed)
ja	~CF & ~ZF	Above (unsigned)
jb	CF	Below (unsigned)

# Conditional Branch Example

```
int absdiff(int x, int y)
{
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
```

absdiff:

pushl %ebp	Setup
movl %esp, %ebp	
movl 8(%ebp), %edx	
movl 12(%ebp), %eax	
cmpl %eax, %edx	
<b>jle .L6</b>	Body1
subl %eax, %edx	
movl %edx, %eax	
<b>jmp .L7</b>	Body2a
.L6:	
subl %edx, %eax	Body2b
.L7:	
popl %ebp	Finish
ret	

# Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
```

- Allows “goto” as means of transferring control
  - Closer to machine-level programming style
- Generally considered bad coding style

`absdiff:`

<code>pushl %ebp</code>	}	Setup
<code>movl %esp, %ebp</code>		
<code>movl 8(%ebp), %edx</code>		
<code>movl 12(%ebp), %eax</code>		
<code>cmpl %eax, %edx</code>	}	Body1
<code>jle .L6</code>		
<code>subl %eax, %edx</code>		
<code>movl %edx, %eax</code>		
<code>jmp .L7</code>	}	Body2a
<code>.L6:</code>		
<code>subl %edx, %eax</code>		
<code>.L7:</code>	}	Body2b
<code>popl %ebp</code>		
<code>ret</code>	}	Finish

# Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
```

absdiff:

pushl %ebp	}	Setup
movl %esp, %ebp		
movl 8(%ebp), %edx		
movl 12(%ebp), %eax		
cmpl %eax, %edx	Body1	
jle .L6		
subl %eax, %edx		
movl %edx, %eax	Body2a	
jmp .L7		
.L6:	Body2b	
subl %edx, %eax		
.L7:	Finish	
popl %ebp		
ret		

# Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
```

absdiff:

pushl %ebp	}	Setup
movl %esp, %ebp		
movl 8(%ebp), %edx		
movl 12(%ebp), %eax		
cmpl %eax, %edx	}	Body1
jle .L6		
subl %eax, %edx		
movl %edx, %eax	}	Body2a
jmp .L7		
.L6:	}	Body2b
subl %edx, %eax		
.L7:	}	Finish
popl %ebp		
ret		

# Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
```

absdiff:

pushl %ebp	}	Setup
movl %esp, %ebp		
movl 8(%ebp), %edx		
movl 12(%ebp), %eax		
cmpl %eax, %edx	}	Body1
jle .L6		
subl %eax, %edx		
movl %edx, %eax	}	Body2a
jmp .L7		
.L6:	}	Body2b
subl %edx, %eax		
.L7:	}	Finish
popl %ebp		
ret		

# Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86 Calling Convention (functions)
- x86-64
- Control: Condition codes
- Conditional branches and moves
- Loops

# “Do-While” Loop Example

## C Code

```
int pcount_do(unsigned x)
{
    int result = 0;
    do {
        result += x & 0x1;
        x >>= 1;
    } while (x);
    return result;
}
```

## Goto Version

```
int pcount_do(unsigned x)
{
    int result = 0;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
    return result;
}
```

- Count number of 1's in argument x (“popcount”)
- Use conditional branch to either continue looping or to exit loop

# “Do-While” Loop Compilation

## Goto Version

```
int pcount_do(unsigned x) {  
    int result = 0;  
loop:  
    result += x & 0x1;  
    x >>= 1;  
    if (x)  
        goto loop;  
    return result;  
}
```

### Registers:

%edx	x
%ecx	result

	movl	\$0, %ecx	#	result = 0
.L2:	movl	%edx, %eax	#	loop:
	andl	\$1, %eax	#	t = x & 1
	addl	%eax, %ecx	#	result += t
	shrl	%edx	#	x >>= 1
	jne	.L2	#	If !0, goto loop

# General “Do-While” Translation

## C Code

```
do  
  Body  
  while ( Test );
```

## Goto Version

```
loop:  
  Body  
  if ( Test )  
    goto loop
```

- **Body:** {
  - Statement<sub>1</sub>;
  - Statement<sub>2</sub>;
  - ...
  - Statement<sub>n</sub>;}

- **Test returns integer**
  - = 0 interpreted as false
  - ≠ 0 interpreted as true

# “While” Loop Example

## C Code

```
int pcount_while(unsigned x) {  
    int result = 0;  
    while (x) {  
        result += x & 0x1;  
        x >>= 1;  
    }  
    return result;  
}
```

## Goto Version

```
int pcount_do(unsigned x) {  
    int result = 0;  
    if (!x) goto done;  
loop:  
    result += x & 0x1;  
    x >>= 1;  
    if (x)  
        goto loop;  
done:  
    return result;  
}
```

- Is this code equivalent to the do-while version?

# General “While” Translation

## While version

```
while ( Test)  
    Body
```



## Do-While Version

```
if ( ! Test)  
    goto done;  
do  
    Body  
    while( Test) ;  
done:
```



## Goto Version

```
if ( ! Test)  
    goto done;  
loop:  
    Body  
    if ( Test)  
        goto loop;  
done:
```

# “For” Loop Example

## C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
    int i;
    int result = 0;
    for (i = 0; i < WSIZE; i++) {
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    return result;
}
```

- Is this code equivalent to other versions?

# “For” Loop Form

## General Form

```
for (Init; Test; Update)  
    Body
```

```
for (i = 0; i < WSIZE; i++) {  
    unsigned mask = 1 << i;  
    result += (x & mask) != 0;  
}
```

### Init

```
i = 0
```

### Test

```
i < WSIZE
```

### Update

```
i++
```

### Body

```
{  
    unsigned mask = 1 << i;  
    result += (x & mask) != 0;  
}
```

# “For” Loop → While Loop

## For Version

```
for (Init; Test; Update)  
    Body
```



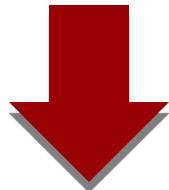
## While Version

```
Init;  
  
while (Test) {  
    Body  
    Update;  
}
```

# “For” Loop → ... → Goto

## For Version

```
for (Init; Test; Update)  
    Body
```

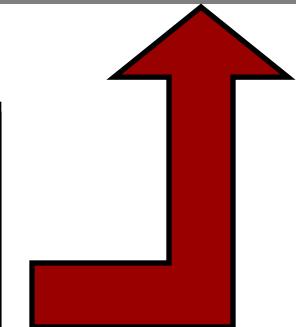


## While Version

```
Init;  
while (Test) {  
    Body  
    Update;  
}
```



```
Init;  
if (!Test)  
    goto done;  
do  
    Body  
    Update  
    while (Test);  
done:
```



# “For” Loop Conversion Example

## Goto Version

### C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
    int i;
    int result = 0;
    for (i = 0; i < WSIZE; i++) {
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    return result;
}
```

- Initial test can be optimized away

```
int pcount_for_gt(unsigned x) {
    int i;
    int result = 0;
    i = 0; Init
    if (!(i < WSIZE)) ! Test
        goto done;
loop:
{
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
}
Update
if (i < WSIZE) Test
    goto loop;
done:
    return result;
}
```

# Summary

## ■ Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches & conditional moves
- Loops

## ■ Next Time

- Switch statements
- Stack
- Call / return
- Procedure call discipline